Package: geess (via r-universe)

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Type Package

Title Modified Generalized Estimating Equations for Small-Sample Data

Version 1.0.1

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Description Analyze small-sample clustered or longitudinal data using modified generalized estimating equations with bias-adjusted covariance estimator. The package provides any combination of three modified generalized estimating equations and 11 bias-adjusted covariance estimators.

Depends R (>= 4.5.0)

Imports MASS (>= 7.3-45)

License GPL (>= 2)

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Suggests testthat (>= 3.0.0)

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Contents

geess *Modified Generalized Estimating Equations for Small-Sample Data*

Description

geess is an extension of geessbin package (Ishii et al., 2024). geess analyzes small-sample clustered or longitudinal data using modified generalized estimating equations (GEE) with bias-adjusted covariance estimator. This function provides any combination of three GEE methods (conventional and two modified GEE methods) and 12 covariance estimators (unadjusted and 11 bias-adjusted estimators).

Usage

```
geess(
  formula,
  family = gaussian,
  data = parent.frame(),
  id = NULL,
  corstr = "independence",
  repeated = NULL,
  beta.method = "GEE",
  SE.method = "SA",
  b = NULL,
  maxitr = 50,
  tol = 1e-05,
  scale.fix = FALSE,
  conf.level = 0.95
)
```

Arguments

formula	Object of class formula: symbolic description of model to be fitted (see documentation of lm and formula for details).
family	Description of the error distribution and link function to be used in the model. The gaussian family accepts the identity link function. The binomial family accepts the links logit and probit. The poisson family accepts the log link function.
data	Data frame.
id	Vector that identifies the subjects or clusters (NULL by default).
corstr	Working correlation structure. The following are permitted: "independence", "exchangeable", "ar1", and "unstructured" ("independence" by default).
repeated	Vector that identifies repeatedly measured variable within each subject or cluster. If repeated = NULL, as is the case in function gee, data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

beta.method	Method for estimating regression parameters (see Details section). The following are permitted: "GEE", "PGEE", and "BCGEE" ("GEE" by default).
SE.method	Method for estimating standard errors (see Details section). The following are permitted: "SA", "MK", "KC", "MD", "FG", "PA", "GS", "MB", "WL", "WB", "FW", and "FZ" ("SA" by default).
b	Numeric vector specifying initial values of regression coefficients. If b = NULL (default value), the initial values are calculated using the ordinary or Firth logistic regression assuming that all the observations are independent.
maxitr	Maximum number of iterations (50 by default).
tol	Tolerance used in fitting algorithm (1e-5 by default).
scale.fix	Logical variable; if TRUE, the scale parameter is fixed at 1 (FALSE by default).
conf.level	Numeric value of confidence level for confidence intervals (0.95 by default).

Details

Details of beta.method are as follows:

- "GEE" is the conventional GEE method (Liang and Zeger, 1986)
- "BCGEE" is the bias-corrected GEE method (Paul and Zhang, 2014; Lunardon and Scharfstein, 2017)
- "PGEE" is the bias reduction of the GEE method obtained by adding a Firth-type penalty term to the estimating equation (Mondol and Rahman, 2019)

Details of SE.method are as follows:

- "SA" is the unadjusted sandwich variance estimator (Liang and Zeger, 1986)
- "MK" is the MacKinnon and White estimator (MacKinnon and White, 1985)
- "KC" is the Kauermann and Carroll estimator (Kauermann and Carroll, 2001)
- "MD" is the Mancl and DeRouen estimator (Mancl and DeRouen, 2001)
- "FG" is the Fay and Graubard estimator (Fay and Graubard, 2001)
- "PA" is the Pan estimator (Pan, 2001)
- "GS" is the Gosho et al. estimator (Gosho et al., 2014)
- "MB" is the Morel et al. estimator (Morel et al., 2003)
- "WL" is the Wang and Long estimator (Wang and Long, 2011)
- "WB" is the Westgate and Burchett estimator (Westgate and Burchett, 2016)
- "FW" is the Ford and Wastgate estimator (Ford and Wastgate, 2017)
- "FZ" is the Fan et al. estimator (Fan et al., 2013)

Descriptions and performances of some of the above methods in the case of binary outcomes can be found in Gosho et al. (2023).

Value

The object of class "geess" representing the results of modified generalized estimating equations with bias-adjusted covariance estimators. Generic function summary provides details of the results.

References

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Examples

```
library(geess)
library(MASS)

# analysis of longitudinal count data usinBCg GEE method with Morel et al. covariance estimator
res <- geess(formula = y ~ trt + period + lbase + lage,
             family = poisson, data = epil, id = subject,
             repeated = period, corstr = "unstructured",
             beta.method = "BCGEE", SE.method = "MB")
print(res)

# hypothesis tests for regression coefficients
summary(res)
```

`sqrtmat` *Square root of nonsymmetric matrix*

Description

`sqrtmat` is used to calculate the square root of $E_i - H_{ii}$, which is an adjustment factor in Kauermann and Carroll-type method.

Usage

```
sqrtmat(M)
```

Arguments

M	Square matrix whose square root is to be computed.

Value

The square root of M

References

Kauermann, G. and Carroll, R. J. (2001). A note on the efficiency of sandwich covariance matrix estimation. *Journal of the American Statistical Association*, 96, 1387–1396, doi:10.1198/016214501753382309.

Index